

Math 2 – Honors
Unit 3 – Quadratic Functions Continued
Lesson 4 → Discriminant & Quadratic Formula

Warm-Up

Name _____
Date _____ Pd _____

- ❖ Solve the following equations by factoring.
- ❖ Graph the equation.

<p>1. $x^2 + x - 6 = 0$ $(x+3)(x-2) = 0$ $x = -3$ $x = 2$</p> <p>Number of Solutions: <u>2</u></p>	<p>2. $x^2 + 6x + 9 = 0$ $(x+3)(x+3) = 0$</p> <p>Number of Solutions: <u>1</u></p>	<p>3. $x^2 + 4 = 0$</p> <p>Number of Solutions: <u>0</u></p>
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➤ Quadratic Equation: $ax^2 + bx + c = 0$

➤ The Discriminant: $b^2 - 4ac$

$$3x^2 + 2x + 1$$

a b c

$$x^2 + 0x + 4$$

$$x^2 + 4 = 0$$

$$\sqrt{x^2} = \sqrt{-4} \quad x = \pm 2i$$

✓ The discriminant is used to determine the number and type of solutions (roots) of a quadratic equation.

- ❖ Using the same three examples from above, find the value of the discriminant and describe the roots.

<p>1. $x^2 + x - 6 = 0$ $b^2 - 4ac$ $(1)^2 - 4(1)(-6)$ $D = 25$ # of Roots: <u>2</u> Type of Roots: <u>Real Rational</u></p>	<p>2. $x^2 + 6x + 9 = 0$ $b^2 - 4ac$ $(6)^2 - 4(1)(9)$ $D = 0$ # of Roots: <u>1</u> Type of Roots: <u>1 Real</u></p>	<p>3. $x^2 + 4 = 0$ $1x^2 + 0x + 4$ $(0)^2 - 4(1)(4)$ $D = -16$ # of Roots: <u>2 imaginary</u> Type of Roots: <u>2 imaginary</u></p>
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➤ Discriminant Conclusions:

Value of the Discriminant: $b^2 - 4ac$	Number and Type of Roots	What does the graph look like?
$b^2 - 4ac$ is POSITIVE and a PERFECT SQUARE $b^2 - 4ac > 0$	2 real	Intersects the x-axis twice
$b^2 - 4ac$ is POSITIVE and NOT a PERFECT SQUARE $b^2 - 4ac > 0$	2 irrational	Intersects the x-axis twice
$b^2 - 4ac = 0$ →	1 Real	Intersects the x-axis once
$b^2 - 4ac$ is NEGATIVE $b^2 - 4ac < 0$	2 complex or 2 imaginary	Never Intersects the x-axis

❖ **Classwork:** Find the value of the discriminant and state the number and type of roots.

Equation	Discriminant	Number and Type of Roots	Rational or Irrational
1. $8x^2 + 2x - 1 = 0$			
2. $x^2 + x + 1 = 0$			
3. $x^2 - 27 = 0$			
4. $x^2 - 8x = -16$			
5. $x^2 + 4x + 9 = 10$			
6. $3x^2 + 5x - 12 = 0$			

➤ Solving Quadratic Equations using the Quadratic Formula

- $ax^2 + bx + c = 0$

- $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

- The Quadratic Formula is used to solve any quadratic equation, especially those that will not factor.

- Examples: Solve using the Quadratic Formula $\rightarrow x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$a=1 \quad b=5 \quad c=5$

$$\frac{-(-5) \pm \sqrt{(-5)^2 - 4(1)(5)}}{2(1)}$$

$$\frac{5 \pm \sqrt{25 - 20}}{2}$$

$$\frac{5 \pm \sqrt{5}}{2}$$

$= 0$

1. $x^2 - 5x - 24 = 0$

$$(x-8)(x+3) = 0$$

$$x = +8, -3$$

$$x^2 - 5/2 x + \frac{100}{16} = 24 + \frac{100}{16}$$

$$\sqrt{\left(x - \frac{10}{4}\right)^2} = \sqrt{\frac{121}{4}}$$

$$x - \frac{10}{4} = \pm \frac{11}{2}$$

$\rightarrow 8$

2. $x^2 + 5x + 5 = 0$

$$x^2 + 5x + \frac{25}{4} = -5 + \frac{25}{4}$$

$$\left(\frac{5}{2}\right)^2 = \frac{25}{4}$$

$$\left(x + \frac{5}{2}\right)^2 = \frac{5}{4}$$

$$x + \frac{5}{2} = \pm \sqrt{\frac{5}{4}}$$

$$x = -\frac{5}{2} \pm \sqrt{\frac{5}{4}}$$

$$x = \frac{10}{4} \pm \frac{11}{2} \rightarrow -3$$

3. $4x^2 + 8x - 1 = 0$

$$\frac{-8 \pm \sqrt{(8)^2 - 4(4)(-1)}}{2(4)}$$

$$\begin{array}{r} 2 \overline{) 180} \\ \underline{2 } 40 \\ \underline{2 } 20 \\ \underline{2 } 10 \\ 5 \end{array}$$

$$\frac{-8 \pm \sqrt{80}}{8} = \frac{-8 \pm 4\sqrt{5}}{8} = \frac{-2 \pm \sqrt{5}}{2} = -1 \pm \sqrt{5/4}$$

5. $x^2 + 25 = 10x$

$$x^2 - 10x + 25 = 0$$

$$(x-5)(x-5) = 0$$

$$x = 5$$

4. $4x^2 = -11x + 20$

$$4x^2 + 11x - 20 = 0$$

$$4x^2 + 11x - 20 = 0$$

$$\frac{-11 \pm \sqrt{(11)^2 - 4(4)(-20)}}{2(4)}$$

$$(x + \frac{11}{4})(x - \frac{5}{4})$$

$$\frac{-11 \pm \sqrt{441}}{8} = \frac{-11 \pm 21}{8}$$

$$\begin{array}{l} -11+21 \\ 8 \\ 5/4 \\ -4 \\ -11-21 \\ 8 \end{array}$$

6. $x^2 + 2x + 4 = 0$

$$\frac{-2 \pm \sqrt{(2)^2 - 4(1)(4)}}{2(1)}$$

$$\begin{array}{r} 2 \overline{) 12} \\ \underline{2 } 6 \\ \underline{2 } 3 \end{array}$$

$$\frac{-2 \pm \sqrt{-12}}{2}$$

$$\frac{-2 \pm 2i\sqrt{3}}{2}$$

$$-1 \pm i\sqrt{3}$$

❖ Solve using the Quadratic Formula → $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

❖ Express answers in simplest radical form or complex form. NO DECIMALS!!

1. $4x^2 + 11x - 20 = 0$

$$x^2 + 11x - 20 = 0$$

$$(x + \frac{16}{4})(x - 5) = 0$$

$$(x + 4)(x - 5/4) = 0$$

$$x = -4 \quad x = 5/4$$

2. $x^2 - 5x - 24 = 0$

$$(x - 8)(x + 3) = 0$$

$$x = 8, -3$$

3. $x^2 - 3x - 3 = 0$

$$\frac{3 \pm \sqrt{(-3)^2 - 4(1)(-3)}}{2(1)}$$

$$\frac{3 \pm \sqrt{21}}{2}$$

4. $x^2 + 5x + 5 = 0$

$$\frac{-5 \pm \sqrt{25 - 4(1)(5)}}{2}$$

$$\frac{-5 \pm \sqrt{5}}{2}$$

5. $x^2 = -x + 1$

$$x^2 + x - 1$$

$$\frac{-1 \pm \sqrt{1 - 4(1)(-1)}}{2(1)}$$

$$\frac{-1 \pm \sqrt{5}}{2}$$

6. $4x^2 + 8x = 1$

$$4x^2 + 8x - 1 = 0$$

$$\frac{-8 \pm \sqrt{64 - 4(4)(-1)}}{8}$$

$$\frac{-8 \pm \sqrt{80}}{8} \quad \frac{-8 \pm 4\sqrt{5}}{8}$$

$$\frac{-2 \pm \sqrt{5}}{2}$$