

Math 2
Unit 3 – Rational Exponents and Solving Quadratics
Lesson 5 → Discriminant & Quadratic Formula

Name _____
 Date _____ Pd _____

- ❖ Solve the following equations by factoring.
- ❖ Graph the equation.

1. $x^2 + x - 6 = 0$	2. $x^2 + 6x + 9 = 0$	3. $x^2 + 4 = 0$
Number of Solutions: <u>2 real</u>	Number of Solutions: <u>1 real</u>	Number of Solutions: <u>0 real</u>

➤ **Quadratic Equation:** $ax^2 + bx + c = 0$

➤ **The Discriminant:** $b^2 - 4ac$

$x^2 + 2x + 3$

2 complex

✓ The discriminant is used to determine the **number** and **type** of solutions (roots) of a quadratic equation.

❖ Using the same three examples from above, find the value of the discriminant and describe the roots.

1. $x^2 + x - 6 = 0$ $A=1 B=1 C=-6$ $b^2 - 4ac = (1)^2 - 4(1)(-6) = 25$ D = <u>25</u> # of Roots: <u>2</u> Type of Roots: <u>real</u>	2. $x^2 + 6x + 9 = 0$ $A=1 B=6 C=9$ $(b)^2 - 4(a)(c) = (6)^2 - 4(1)(9) = 0$ D = <u>0</u> # of Roots: <u>1</u> Type of Roots: <u>real</u>	3. $x^2 + 4 = 0$ $A=1 B=0 C=4$ $(b)^2 - 4(a)(c) = (0)^2 - 4(1)(4) = -16$ D = <u>-16</u> # of Roots: <u>2 imaginary</u> Type of Roots: <u>imaginary complex</u>
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➤ **Discriminant Conclusions:**

Value of the Discriminant: $b^2 - 4ac$	Number and Type of Roots	What does the graph look like?
$b^2 - 4ac$ is POSITIVE and a PERFECT SQUARE $b^2 - 4ac > 0$	2 real rational (no radical)	Intersects the x-axis twice
$b^2 - 4ac$ is POSITIVE and NOT a PERFECT SQUARE $b^2 - 4ac > 0$	2 real irrational	Intersects the x-axis twice
$b^2 - 4ac = 0$	1 real solution	Intersects the x-axis once
$b^2 - 4ac$ is NEGATIVE $b^2 - 4ac < 0$	0 real 2 imaginary	Never intersects the x-axis

❖ **Classwork:** Find the value of the discriminant and state the number and type of roots.

Equation	Discriminant	Number and Type of Roots	Rational or Irrational
$A=8 \ B=2 \ C=-1$ 1. $8x^2 + 2x - 1 = 0$	$b^2 - 4ac$ $(2)^2 - 4(8)(-1)$ $= 36$	2 real rational	
2. $x^2 + x + 1 = 0$	SKIP		
3. $x^2 - 27 = 0$			
4. $x^2 - 8x = -16$			
$x^2 + 4x - 1 = 0$ 5. $x^2 + 4x + 9 = 10$ $-10 \ -10$		$A=1 \ B=4 \ C=-1$ $(4)^2 - 4(1)(-1)$ $= 20$	2 real irrational
6. $3x^2 + 5x - 12 = 0$	$A=3 \ B=5 \ C=-12$ $(5)^2 - 4(3)(-12)$ $= 169$	1 real rational	

➤ Solving Quadratic Equations using the Quadratic Formula

• $ax^2 + bx + c = 0$

• $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

• The Quadratic Formula is used to solve any quadratic equation, especially those that will not factor.

• Examples: Solve using the Quadratic Formula $\rightarrow x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

1. $x^2 - 5x - 24 = 0$ $(x-8)(x+3) = 0$ $x = 8 \ x = -3$ $A=1 \ B=-5 \ C=-24$	$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $\frac{-(-5) \pm \sqrt{(-5)^2 - 4(1)(-24)}}{2(1)}$ $\frac{5 \pm \sqrt{121}}{2} = \frac{5 \pm 11}{2}$ $\frac{5+11}{2} = 8 \quad \frac{5-11}{2} = -3$	2. $x^2 + 5x + 5 = 0$ $A=1 \ B=5 \ C=5$ $\frac{-5 \pm \sqrt{5^2 - 4(1)(5)}}{2(1)}$ $\frac{-5 \pm \sqrt{5}}{2}$
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$$3. 4x^2 + 8x - 1 = 0$$

$$A=4 \quad B=8 \quad C=-1$$

$$\frac{-8 \pm \sqrt{(8)^2 - 4(4)(-1)}}{2(4)} = \frac{-8 \pm \sqrt{80}}{8}$$

$$\frac{-8 \pm 4\sqrt{5}}{8} = \frac{-2 \pm \sqrt{5}}{2}$$

$$\begin{array}{r} 2 \overline{)80} \\ \underline{2 \ 40} \\ 2 \ 00 \\ \underline{2 \ 10} \\ 10 \end{array}$$

$$4. 4x^2 = -11x + 20$$

$$4x^2 + 11x - 20 = 0$$

$$x^2 + 11x - 20 = 0$$

$$(x+11)(x-5) = 0$$

$$(x+4)(4x-5) = 0$$

$$x = -4 \quad x = 5/4$$

$$A=4 \quad B=11 \quad C=-20$$

$$\frac{-11 \pm \sqrt{(11)^2 - 4(4)(-20)}}{2(4)}$$

$$\frac{-11 \pm \sqrt{441}}{8} = \frac{-11 \pm 21}{8}$$

$$\frac{-11+21}{8} = \frac{5}{4} \quad \frac{-11-21}{8} = -4$$

$$5. x^2 + 25 = 10x$$

$$x^2 - 10x + 25 = 0$$

$$(x-5)(x-5) = 0$$

$$x = 5$$

$$\frac{10 \pm \sqrt{(10)^2 - 4(1)(25)}}{2}$$

$$\frac{10}{2} = 5$$

$$6. x^2 + 2x + 4 = 0$$

$$A=1 \quad B=2 \quad C=4$$

$$\frac{-2 \pm \sqrt{(2)^2 - 4(1)(4)}}{2(1)} = \frac{-2 \pm \sqrt{-12}}{2} = \frac{-2 \pm 2i\sqrt{3}}{2}$$

$$-1 \pm i\sqrt{3}$$

$$x = \left\{ \begin{array}{l} -1 + i\sqrt{3} \\ -1 - i\sqrt{3} \end{array} \right\}$$

$$\begin{array}{r} 2 \overline{)12} \\ \underline{2 \ 6} \\ 6 \end{array}$$