

$$3. \quad x^2 + 12x + 43 = 0$$

$$-43 \quad -43$$

$$x^2 + 12x + \underline{36} = -43 + \underline{36}$$

$$\sqrt{(x+6)^2} = \sqrt{-7}$$

$$x+6 = \pm\sqrt{-7}$$

$$x+6 = \pm i\sqrt{7}$$

$$-6$$

$$-6$$

$$x = -6 \pm i$$

$$\pm i\sqrt{7}$$

$$4. \quad 3x^2 - 6x - 45 = 0$$

- 1) **BEGIN** with $ax^2 + bx + c = 0$ and **MULTIPLY** "a" to "c"
- 2) **REWRITE** $x^2 + bx = -c \cdot a$
- 3) $x^2 + bx + \underline{\quad} = -c \cdot a + \underline{\quad}$
- 4) **COMPLETE THE SQUARE** by taking half of b ; square it and **ADD IT TO BOTH SIDES** of the equation in the blanks.
- 5) **FACTOR** the perfect square trinomial.
- 6) Take the **SQUARE ROOT** of both sides. Don't forget to include a \pm to create 2 solutions.
- 7) **SOLVE** both equations. **SIMPLIFY** all irrational and complex solutions.
- 8) **DIVIDE** by "a" and **REDUCE** all final solutions.

$$5. \quad 3x^2 + 10x - 8 = 0$$

$$+8 \quad +8$$

$$3x^2 + 10x = 8$$

$$6. \quad 4x^2 - 8x + 3 = 0$$

$$x^2 - 2x + \frac{3}{4} = 0$$

$$\left(x - \frac{2}{2}\right)\left(x - \frac{3}{4}\right)$$

$$\left(x - \frac{1}{2}\right)\left(x - \frac{3}{4}\right)$$

$$(2x-1)\left(2x-\frac{3}{2}\right)$$

$$x = \frac{1}{2} \quad x = \frac{3}{4}$$

$$7. \quad 4x^2 - 16x + 71 = 0$$

$$8. \quad 3x^2 + 6x - 4 = 0$$

pg. 13 # 5 $3x^2 + 10x - 8 = 0$
 $\quad\quad\quad +8 \quad +8$

$$3x^2 + 10x = +8$$

$$3\left(x^2 + \frac{10}{3}x + \sqrt{\frac{100}{36}}\right) = 8 + 3 \cdot \frac{100}{36}$$

$$\frac{10}{3} \cdot \frac{1}{2} = \left(\frac{10}{6}\right)^2 = \frac{100}{36}$$

$$\cancel{3}\left(x + \frac{10}{6}\right)^2 = \frac{49}{3} \cdot \frac{1}{3}$$

$$\sqrt{\left(x + \frac{10}{6}\right)^2} = \sqrt{\frac{49}{9}}$$

$$x + \frac{10}{6} = \pm \frac{7}{3}$$

$$x = \frac{7}{3} - \frac{10}{6} \quad \Bigg| \quad -\frac{7}{3} - \frac{10}{6}$$

$$\quad\quad\quad \frac{2}{3} \quad\quad\quad -4$$

$$3x^2 + 10x - 8$$

$$x^2 + 10x - 24$$

$$\frac{(x+12)(x-2)}{3 \quad 3}$$

$$(x+4)(3x-2)$$

$$x = -4 \quad x = \frac{2}{3}$$

SOLVE BY COMPLETING THE SQUARE:

<p>1. $x^2 + 14x - 51 = 0$ $\quad \quad \quad +51 \quad +51$ $x^2 + 14x + 49 = 51 + 49$ $\sqrt{(x+7)^2} = \sqrt{100}$ $x+7 = \pm 10$ $x+7 = +10 \quad x+7 = -10$ $x = 3 \quad x = -17$</p>	<p>2. $x^2 - 12x + 23 = 0$ $\quad \quad \quad -23 \quad -23$ $x^2 - 12x + 36 = -23 + 36$ $\sqrt{(x-6)^2} = \sqrt{13}$ $x-6 = \pm \sqrt{13}$ $x = 6 \pm \sqrt{13}$</p>
<p>3. $x^2 - 4x + 6 = 0$ $\quad \quad \quad -6 \quad -6$ $x^2 - 4x + 4 = -6 + 4$ $\sqrt{(x-2)^2} = \sqrt{-2}$ $x-2 = \pm i\sqrt{2}$ $x = 2 \pm i\sqrt{2}$</p>	<p>4. $x^2 - 10x + 18 = 0$ $\quad \quad \quad -18 \quad -18$ $x^2 - 10x + 25 = -18 + 25$ $\sqrt{(x-5)^2} = \sqrt{7}$ $x-5 = \pm \sqrt{7}$ $x = 5 \pm \sqrt{7}$</p>
<p>5. $x^2 + 18x - 40 = 0$</p>	<p>6. $4x^2 + 4x + 36 = 0$ $\quad \quad \quad -36 \quad -36$ $4x^2 + 4x = -36$ $4(x^2 + x + 4) = -36 + 4 \cdot 4$ $(\frac{1}{2})^2 = \frac{1}{4}$ $4(x + \frac{1}{2})^2 = -\frac{35}{4}$ $x + \frac{1}{2} = \pm i\sqrt{\frac{35}{4}}$ $x = -\frac{1}{2} \pm i\sqrt{\frac{35}{4}}$</p>
<p>7. $x^2 + 2x + 20 = 0$ $\quad \quad \quad -20 \quad -20$ $x^2 + 2x + 1 = -20 + 1$ $\sqrt{(x+1)^2} = \sqrt{-19}$ $x+1 = \pm i\sqrt{19}$ $x = -1 \pm i\sqrt{19}$</p>	<p>8. $3x^2 + 12x + 21 = 0$ $\quad \quad \quad -21 \quad -21$ $3x^2 + 12x = -21$ $3(x^2 + 4x + 4) = -21 + 3 \cdot 4$ $3(x+2)^2 = -9$ $\sqrt{(x+2)^2} = \sqrt{-3}$ $x+2 = \pm i\sqrt{3}$</p>