

QUIZ DATES: \_\_\_\_\_ & \_\_\_\_\_

TEST DATE: \_\_\_\_\_

Math 2

Name \_\_\_\_\_

Unit 3 – Quadratic Functions Continued

Date \_\_\_\_\_ Pd \_\_\_\_\_

Lesson 1 → Simplifying Square Roots

PERFECT SQUARES

NUMBER MULTIPLIED	PERFECT SQUARES	NUMBER MULTIPLIED	PERFECT SQUARES	NUMBER MULTIPLIED	PERFECT SQUARES
1 X 1 =	1	7 X 7 =	49	13 X 13 =	169
2 X 2 =	4	8 X 8 =	64	14 X 14 =	196
3 X 3 =	9	9 X 9 =	81	15 X 15 =	225
4 X 4 =	16	10 X 10 =	100	16 X 16 =	256
5 X 5 =	25	11 X 11 =	121	17 X 17 =	289
6 X 6 =	36	12 X 12 =	144	18 X 18 =	324

SQUARE ROOTS and CUBE ROOTS

Taking the square root of a number is the inverse of raising the number to the second power.

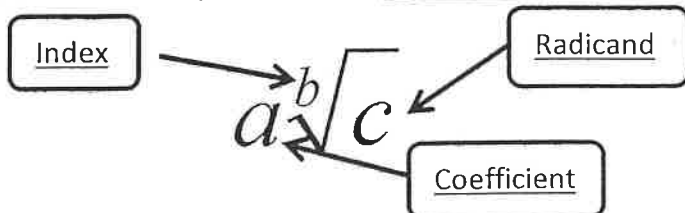
For example: If  $3^2 = 9$ , then  $\sqrt{9} = 3$ . For example: If  $7^2 = 49$ , then  $\sqrt{49} = 7$ .

Taking the cube root of a number is the inverse of raising the number to the third power.

For example: If  $3^3 = 27$ , then  $\sqrt[3]{27} = 3$ . For example: If  $7^3 = 343$ , then  $\sqrt[3]{343} = 7$ .

PARTS OF A RADICAL

An expression that contains a square root is a \_\_\_\_\_. It can have three parts.



➤ Simplify the following radical expressions.

$\sqrt{100} = 10$        $3\sqrt{121} = 3 \cdot 11 = 33$        $-\sqrt{225} = -15$        $-2\sqrt{144} = -2 \cdot 12 = -24$   
 $\sqrt{25} = 5$        $7\sqrt{81} = 7 \cdot 9 = 63$        $\pm\sqrt{49} = \pm 7$        $\pm 9\sqrt{9} = \pm 9 \cdot 3 = \pm 27$

➤ What is the radicand is not a perfect square but has a factor that is a perfect square?

• Simplify:  $\sqrt{24} =$

$$\frac{\sqrt{4} \cdot \sqrt{6}}{2\sqrt{6}}$$

$$2\sqrt{6}$$

$$\begin{array}{r} 2 \overline{)24} \\ \underline{2 \ 12} \\ 2 \ 6 \\ \underline{2 \ 6} \\ 0 \end{array}$$

$$\begin{array}{r} 3 \overline{)24} \\ \underline{3 \ 9} \\ 2 \ 4 \\ \underline{2 \ 4} \\ 0 \end{array}$$

$$\begin{array}{r} 2 \overline{)24} \\ \underline{2 \ 12} \\ 2 \ 6 \\ \underline{2 \ 6} \\ 0 \end{array}$$

What is the highest factor of 24 that is also a perfect square? \_\_\_\_\_. Therefore,  $24 =$  \_\_\_\_\_

• Simplify:  $\sqrt{32} =$

$$4\sqrt{2} \quad 2 \cdot 2\sqrt{2} \quad 4\sqrt{2}$$

What is the highest factor of 32 that is also a perfect square? \_\_\_\_\_. Therefore,  $32 =$  \_\_\_\_\_

• Simplify:  $\sqrt{54}$

Prime #'s : 2, 3, 5, 7, 11, 13, 17, 19, 23, 29...

What is the highest factor of 54 that is also a perfect square? \_\_\_\_\_. Therefore,  $54 =$  \_\_\_\_\_

$$\begin{array}{r} 2 \overline{)54} \\ \underline{2 \ 27} \\ 3 \ 9 \\ \underline{3 \ 9} \\ 0 \end{array}$$

$$\begin{array}{r} 3 \overline{)54} \\ \underline{3 \ 18} \\ 3 \ 6 \\ \underline{3 \ 6} \\ 0 \end{array}$$

$$\begin{array}{r} 1 \overline{)54} \\ \underline{1 \ 27} \\ 2 \ 7 \\ \underline{2 \ 6} \\ 1 \end{array}$$

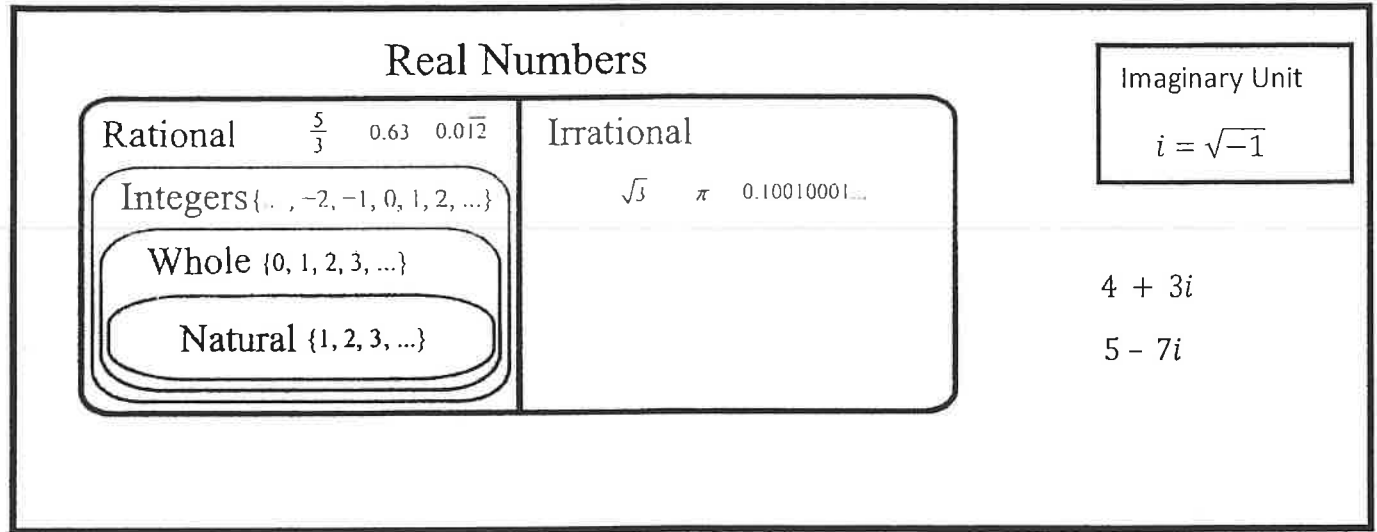
**PERFECT SQUARES:**

➤ Classwork:

1. $\sqrt{18}$ $3\sqrt{2}$	2. $\sqrt{20}$ $2\sqrt{5}$	3. $\sqrt{40}$ $2\sqrt{10}$	4. $\sqrt{50}$ $5\sqrt{2}$	5. $\sqrt{63}$ $3\sqrt{7}$
6. $\pm\sqrt{63}$ $\pm 3\sqrt{7}$	7. $\sqrt{48}$ $4\sqrt{3}$	8. $\sqrt{98}$ $7\sqrt{2}$	9. $\sqrt{75}$ $2 \cdot 5\sqrt{3}$ $10\sqrt{3}$	10. $\frac{1}{2}\sqrt{256}$ $\frac{1}{2} \cdot 16 = 8$

<p>5 ← <math>\frac{5\sqrt{50}}{5}</math></p> <p><math>5 \cdot 5\sqrt{2}</math></p> <p><math>25\sqrt{2}</math></p>	2. $3\sqrt{32}$	3. $-\sqrt{52}$	<p>4. ← <math>\frac{\sqrt{99}}{3}</math></p> <p><math>\frac{1}{3} \cdot 3\sqrt{11}</math></p> <p><math>\frac{1}{2}\sqrt{11}</math></p>	5. $\pm\sqrt{48}$
6. $2\sqrt{18}$	7. $-4\sqrt{12}$	8. $5\sqrt{24}$	<p>9. ← <math>\frac{5\sqrt{20}}{5}</math></p> <p><math>-\frac{1}{2} \cdot 2\sqrt{5}</math></p> <p><math>-\sqrt{5}</math></p> <p><math>-\sqrt{5}</math></p>	10. $5\sqrt{500}$
11. $-\sqrt{44}$	12. $12\sqrt{60}$	13. $-10\sqrt{80}$	14. $\frac{1}{2}\sqrt{8}$	15. $\pm\sqrt{12}$
16. $3\sqrt{250}$	<p>17. ← <math>-\frac{4}{5}\sqrt{50}</math></p> <p><math>-\frac{4}{5} \cdot 5\sqrt{2}</math></p> <p><math>-4\sqrt{2}</math></p>	18. $\pm 7\sqrt{90}$	19. $3\sqrt{10}$	<p>20. ← <math>\pm 3\sqrt{117}</math></p> <p><math>\pm 2 \cdot 3\sqrt{13}</math></p> <p><math>\pm 6\sqrt{13}</math></p>

# COMPLEX NUMBERS



**COMPLEX NUMBERS:** the set of numbers including the Real Numbers and the imaginary unit,  $i$ . Complex number are written in the form  $a + bi$  where  $a$  is the real part and  $bi$  is the imaginary part.

**IMAGINARY UNIT:**

Some polynomial equations have complex (non-real) solutions, when a negative number is under the radical symbol.

For example: there is no real solution to  $\sqrt{-16}$  or  $\sqrt{-36}$ .

Mathematicians created a new system of numbers using the imaginary unit,  $i$ , defined as  $i = \sqrt{-1}$ . With this new system of numbers, radicals of negative numbers can now be simplified!

Therefore:  $i = \sqrt{-1}$

Simplify:  $\sqrt{-16} = \underline{4i}$

$\sqrt{-36} = \underline{6i}$

$\frac{2 \cdot 20}{5 \cdot 2} = 2$

$\sqrt{-20} = \underline{2i\sqrt{5}}$

$\sqrt{-27} = \underline{\hspace{2cm}}$

$\sqrt{-45} = \underline{\hspace{2cm}}$

$\frac{5\sqrt{-75}}{5\sqrt{3}} = \frac{5i\sqrt{3}}{5\sqrt{3}} = 5i\sqrt{3}$

➤ Determine whether each number is **rational** or **irrational**:

6	$\frac{5}{6}$	$\sqrt{6} + \sqrt{3}$	$1 - \pi$	$5 + \sqrt{6}$
0.6	$\pi$	$\frac{\pi}{2}$	$\frac{\sqrt{6}}{\sqrt{3}}$	0.45
-6	0.456789...	$4 + \sqrt{3}$	0	$0.\overline{273}$

➤ Express each number in terms of **i** and then **simplify**:

1. $\sqrt{-36}$	2. $\sqrt{-100}$	3. $-\sqrt{-81}$	4. $2\sqrt{-49}$
5. $\frac{1}{8}\sqrt{-64}$	6. $\frac{-2}{3}\sqrt{-9}$	7. $\frac{3}{4}\sqrt{-144}$	8. $\frac{1}{3}\sqrt{-25}$
9. $\sqrt{-\frac{1}{4}}$	10. $\sqrt{-\frac{16}{25}}$ $i \cdot \frac{4}{5}$ <span style="border: 1px solid black; padding: 2px;"><math>\frac{4}{5}i</math></span>	11. $4\sqrt{-\frac{49}{64}}$ $\frac{4i \cdot 7}{8}$ <span style="border: 1px solid black; padding: 2px;"><math>\frac{28}{8}i</math></span>	12. $\frac{3}{5}\sqrt{-\frac{100}{9}}$
13. $\sqrt{-3}$	14. $\sqrt{-29}$	15. $3\sqrt{-11}$	16. $-\sqrt{-10}$ $-i\sqrt{10}$
17. $\sqrt{-20}$	18. $-\sqrt{-28}$ $-i \cdot 2\sqrt{7}$ <span style="border: 1px solid black; padding: 2px;"><math>-2i\sqrt{7}</math></span>	19. $2\sqrt{-75}$ $2 \cdot 5i\sqrt{3}$ <span style="border: 1px solid black; padding: 2px;"><math>10i\sqrt{3}</math></span>	20. $5\sqrt{-8}$
21. $3\sqrt{-98}$	22. $-2\sqrt{-75}$	23. $\pm\sqrt{-45}$	24. $\frac{3\sqrt{7}}{\sqrt{-28}}$